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information

1. AGENCY USE ONLY (Leave blank)		2. REPORT DATE February 1999	3. REPORT TYPE AND DATES COVERED FINAL REPORT 15 Feb 97 - 14 Nov 98
4. TITLE AND SUBTITLE MECHANICAL BEHAVIOR OF GRANULAR/PARTICULATE MEDIA REINFORCED WITH FIBERS			5. FUNDING NUMBERS F49620-97-1-0109
6. AUTHOR(S) RADOSLW MICHALOWSKI			61102F 2302/CS
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) THE JOHNS HOPKINS UNIVERSITY DEPARTMENT OF CIVIL ENGINEERING 3400 N. CHARLES STREET BALTIMORE, MD 21218-2686			8. PERFORMING ORGANIZATION REPORT NUMBER
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) AIR FORCE OFFICE OF SCIENTIFIC RESEARCH (AFOSR) 801 N. RANDOLPH STREET, ROOM 732 ARLINGTON, VA 22203-1977			10. SPONSORING/MONITORING AGENCY REPORT NUMBER
11. SUPPLEMENTARY NOTES			
12a. DISTRIBUTION AVAILABILITY STATEMENT APPROVED FOR PUBLIC RELEASE, DISTRIBUTION IS UNLIMITED			12b. DISTRIBUTION CODE
13. ABSTRACT (Maximum 200 words) Fiber-reinforced granular composites (for instance, fiber-reinforced sand) are considered as construction materials for such applications as subgrades of airfields and roads, aircraft parking facilities, etc. An investigation into the mechanical behavior of granular/particulate media with fibrous inclusions was carried out. This investigation was built on the results of a previous study. Fiber-reinforced granular material was considered as a composite, and a mathematical homogenization scheme was used to arrive at its macroscopic properties. The issues related to micromechanic behavior, leading to anisotropy and hardening/softening at the macroscopic level of description, were at the core of this investigation. This research produced a material model which accurately describes the behavior of fiber-reinforced soils at failure. The research was terminated before its conclusion, because of the elimination of the Particulate Mechanics program at the AFOSR.			
14. SUBJECT TERMS MECHANICAL FIBERS			15. NUMBER OF PAGES 6
			16. PRICE CODE
17. SECURITY CLASSIFICATION OF REPORT UNCLASSIFIED	18. SECURITY CLASSIFICATION OF THIS PAGE UNCLASSIFIED	19. SECURITY CLASSIFICATION OF ABSTRACT UNCLASSIFIED	20. LIMITATION OF ABSTRACT

**Final Report**

submitted to

**Air Force Office of Scientific Research**

Directorate of Aerospace Studies  
(Program: Particulate Materials)

**Mechanical Behavior of Granular/Particulate Media  
Reinforced with Fibers**

(Grant No. F49620-97-1-0109)

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February 1999

19990302050

## Summary

Fiber-reinforced granular composites (for instance, fiber-reinforced sand) are considered as construction materials for such applications as subgrades of airfields and roads, aircraft parking facilities, etc. An investigation into the mechanical behavior of granular/particulate media with fibrous inclusions was carried out. This investigation was built on the results of a previous study.

Fiber-reinforced granular material was considered as a composite, and a mathematical homogenization scheme was used to arrive at its macroscopic properties. The issues related to micromechanic behavior, leading to anisotropy and hardening/softening at the macroscopic level of description, were at the core of this investigation. This research produced a material model which accurately describes the behavior of fiber-reinforced soils at failure. The research was terminated before its conclusion, because of the elimination of the Particulate Mechanics program at the AFOSR.

## Objectives

The following were the objectives of this research: (a) progress in understanding of the elasto-plastic behavior of fibrous composites with a granular matrix, (b) identification of the most important mechanisms for fiber-matrix interaction (load transfer and distribution), (c) mathematical description of the elasto-plastic stress-strain behavior of the composite at the macroscopic level (homogenization of microstructural interactions), and a more general description of failure of anisotropic granular composites, and (d) collection of experimental evidence for validation of the mathematical description.

## Accomplishments and New Findings

The first stage of the research concentrated mainly on the second objective (identification of the most important mechanisms for fiber-matrix interaction). The main results are described partly in papers listed in section: Publications. The research led to deriving of the analytic expressions for the failure criterion of isotropic fiber-reinforced granular materials, and to experimentally validating this criterion. The failure surface in the  $q, p, \tau_{xy}$ -stress space [ $q = (\sigma_x - \sigma_y)/2$ ,  $p = (\sigma_x + \sigma_y)/2$ ] for the isotropic composite is shown in Fig. 1 (stresses are normalized by  $\rho\sigma_0$ ,  $\rho$  - volumetric fiber content,  $\sigma_0$  - fiber yield stress).

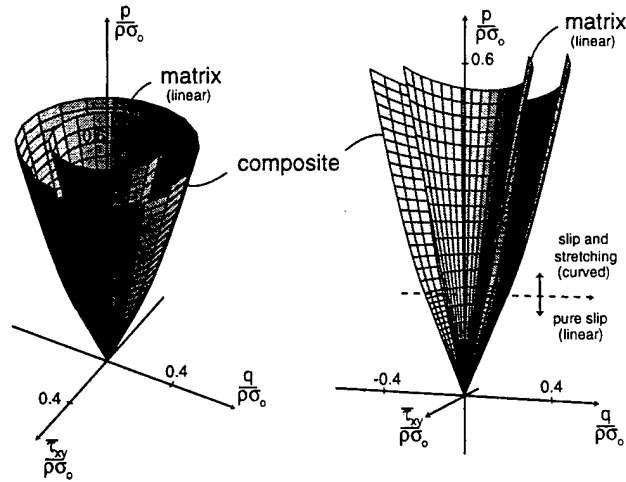


Figure 1. Failure surface for isotropic fiber-reinforced sand.

The mathematical description was extended to anisotropic soils. The process of composite homogenization is considerably more elaborate for an anisotropic distribution of fibers, but the calculations were carried out using a numerical optimization scheme, and the failure surface produced is shown in Fig. 2.

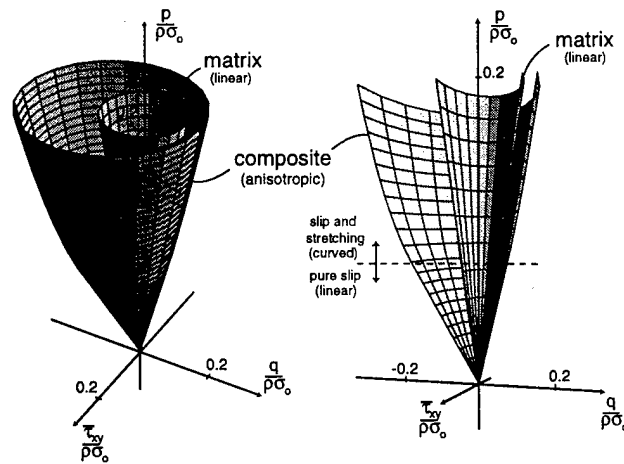


Figure 2. Failure surface for anisotropic fiber-reinforced sand.

Laboratory tests indicated a distinct kinematic (anisotropic) hardening effect. This effect can be described only approximately with the existing model. Preliminary results of calculations superimposed on the laboratory test results are shown in Fig. 3. More realistic mechanisms of

load transfer (from the matrix material to the fibers) need to be identified to obtain a better description, particularly in the early stages of the deformation process. Recent considerations revealed that a more elaborate hardening/softening law on the fiber-matrix interface needs to be used before the process of the composite strength mobilization can be captured. Other research issues identified as important are: instability of the fiber slip, scale effects caused by the nature of the stress-displacement law of fiber slip in addition to scale effects caused by the fiber aspect ratio, and influence of fiber stiffness on the behavior of the composite.

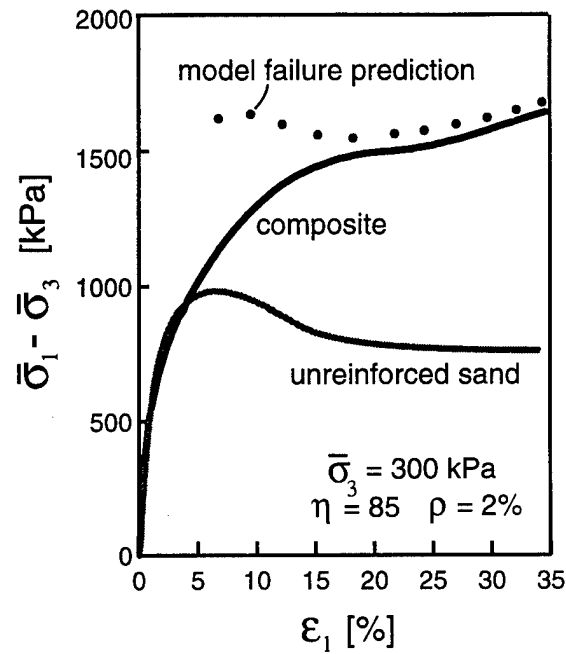


Figure 3. Kinematic hardening effect for fiber-reinforced sand. Comparison of a laboratory test with preliminary calculations.

In addition, a reinforcement with continuous filament was considered. The load transfer process in the latter case is similar to the *belt friction* effect, and such composite can be very effective. This type of composite was to be further explored in the last funding period. The two types of composites (fiber-reinforced and continuous filament-reinforced) are shown schematically in Fig. 4. An example of a cross-section of the yield condition for continuous filament-reinforced sand is presented in Fig. 5.

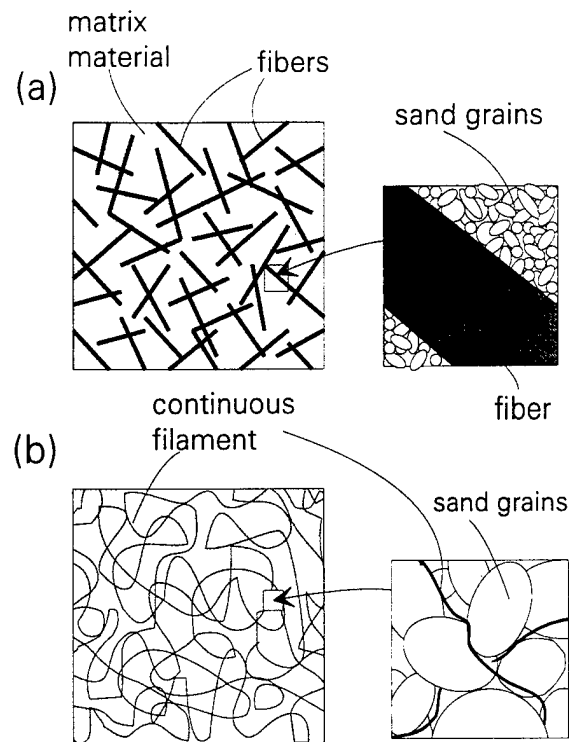


Figure 4. Reinforced granular composites: (a) Fiber reinforcement, and (b) Continuous thin filament.

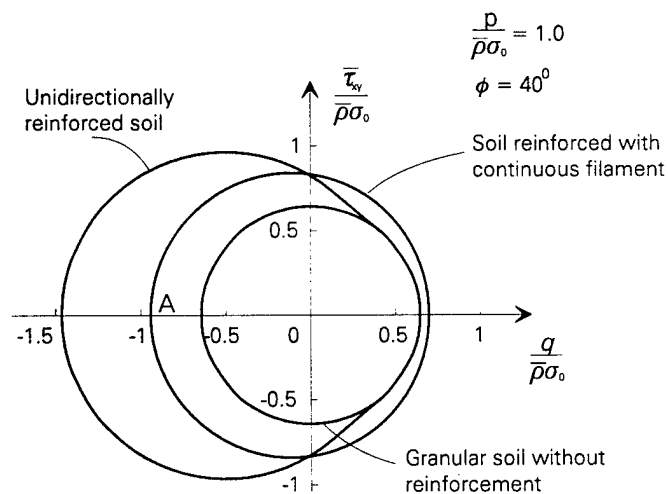


Figure 5. Strength of filament-reinforced soil: Cross section of the yield criterion.

## Students Supported

There have been two students supported by this research project: Jan Čermák, who completed his Ph.D. dissertation in 1997 (thesis title: "Limit Behavior of Fiber-Reinforced Granular Soils"); and Liangzhi You, who is expected to complete his research toward his Ph.D. degree in 1999.

## Publications

The main results are presented in the following papers:

Michalowski, R.L. and Čermák, J. (1997). *Anisotropic strength of fiber-reinforced soils*, Numerical Models in Geomechanics, S. Pietruszczak, G.N. Pande, eds., Proc. VI Intl. Symp., Montreal 2-4 July, 233-238.

Michalowski, R.L. (1997). *Mechanical behavior of granular/particulate media reinforced with fibers*. in: Selected Research in Particulate Materials and Shock Physics, Air Force Office of Scientific Research, 3-5 Feb., Landsdowne, VA, 65-68.

Čermák, J. and Michalowski, R.L. (1997). *Limit behavior of fiber-reinforced granular composites*, Mechanics of Deformation and Flow of Particulate Materials, C.S. Cheng, A. Misra, R.Y. Liang, M. Babic, eds., Proc. ASME Symposium, Evanston, June-July, 149-158.

Michalowski, R.L. (1998). *Kinematic hardening of fiber-reinforced granular composites*. In: Engineering Mechanics: A Force for the 21st. Century. Proc. of the 12th. Engineering Mechanics Conference (ASCE), La Jolla, May 1998, 1343-1346.

Michalowski, R.L. (1998). *Anisotropic Strength of reinforced soil*. Selected Research in Particulate Materials and Shock Physics, Air Force Office of Scientific Research, San Diego, May 1998.

## Termination of the Project

This project was terminated in September 1998 due to elimination of the Particulate Mechanics program at AFOSR.